

i fjes l a[; k, i

9.1 Hkiedk

vkius l [; kvka dk vè; ; u vius ifjošk dh olryka oQ fxuus ls ikjlk fd; kA bl dk; z ea iżks dh xbz l [; kvka dks x.ku l [; k, i (counting numbers); k ikNr l [; k, i (natural numbers) dgk x; k FKA ; s g1] 2] 3] 4] --A ikNr l [; kvka ea0 dks l fEfyr djus ij ges iwz l [; k, i (whole numbers), vFkk~0] 1] 2] 3] --- iklr gbl oQ ckn] i wkked (integers) iklr djusoQ fy,] iwz l [; kvka ea ikNr l [; kvka oQ ½. kkRedk (negatives) dks l fEfyr fd; k x; kA --- &3] &2] &1] 0] 1] 2] 3 --- i wkked gbl iżdkj] geus l [; k i ¼fr (number system) dks ikNr l [; kvka ls iwz l [; kvka rd vkj i wz l [; kvka ls i wkkedard foLrr fd; kA



vkidk fHkkuka (fractions) ls Hkh ifjp; djk; k x; k FKA ; s $\frac{vak}{gj}$ numerator denominator , oQ iżdkj dh l [; k, i gksk gbl tgk vek ; k rks 0 ; k , d èkukRed i wkked gksk gsrFkk gj] , d èkukRed i wkked gksk gbl vki us nks fHkkuka dh ryuk dh] muoQ lerY; (equivalent) : i (fHkkuka) Kkr fd, rFkk mu ij l Hkh pkjkavkèkkjHkr l fØ; kvka; ks] 0; odyu (?kvkuk)] xqku vkj foHkktu dk vè; ; u fd; kA

bl vè; k; ej ge l [; k i ¼fr dk vkj vksx foLrkj djka ge ifjes l [; kvka (rational numbers) dh voèkkj.kk dk ifjp; nadj mu ij ;ks] 0; odyu] xqku vkj foHkktu (Hkkx) dh l fØ; k, i djuk l h[ksA

9.2 i fjes l [; kvka dh vko'; drk

igys ge nsk pph gbl fd l iżdkj l [; kvka ls l c½ foijhr (opposite) fLFkfr; kA dks 0; Dr djusoQ fy, i wkkedk dk iżks fd; k tk l drk gbl mnkgj. kFKj ;fn , d LFkku oQ nkbs vkj 3 km njh dks 3 ls 0; Dr fd; k tk,] rks ml h LFkku ls ckb±vkj dh 5 km njh dks &5

I s0; Dr fd;k tk l drk g; ; fn 150 # ds ykHk dks 150 I s0; Dr fd;k tk,] rks 100 # dh gkf u dks 100 I s0; Dr fd;k tk l drk g; bl h i dkj dh vud fLFkr; k gksh g; ftueafHkluRed I ;k, j (fHklu) I e½ gksh g; ge I epzry I s Åij 750 m dh Åpkbz dks $\frac{3}{4}$ km I s0; Dr dj l drsg; D; k ge I epzry I suhps 750 m dh xgjkbz dks km e;0; Dr dj l drsg; D; k ge I epzry I suhps $\frac{3}{4}$ km dh xgjkbz dks $\frac{63}{4}$ I s0; Dr dj l drsg; ge n[k l drsg; fd $\frac{63}{4}$ u rks, d i wkkd g; vks u gh , d fHkluA , dh I ;kvka dks I fEfyr djus o; fy,] ges I ;k i ½fr dks folrr djus dh vko'; drk g;

9.3 ifjes I ;k, j D; k g;

'kChn ^ifjes * (rational) dh mRifluk] in ^vujkr* (ratio) I sg;g; vki tkurs g;fd vujkr 3 % 2 dks $\frac{3}{2}$ Hkh fy[kk tk l drk g; ; gk; 3 vks 2 i kN r I ;k, j g;



bl h i dkj] nks i wkkdks p vks q (q = 0) o; vujkr p:q dks $\frac{p}{q}$ fy[kk tk l drk g; ; gh og : i g;ft I e; ifjes I ;k, j 0; Dr dh tkrh g; , d ifjes I ;k dks, dh I ;k o; : i e; ifjHkfk"kr fd;k tkrk g; ft I s $\frac{p}{q}$, o; : i e;0; Dr fd;k tk l o; tgk p vks q i wkkd g; rFkkq = 0 g; bl i dkj] $\frac{4}{5}$, d ifjes I ;k g; ; gk; p = 4 g; vks q = 5 g;

D; k $\frac{63}{4}$ Hkh , d ifjes I ;k g; gk; D; kfd p = 63 vks q = 4 i wkkd g;

- vki us $\frac{3}{8}, \frac{4}{8}, 1\frac{2}{3}$, bR; kfn t\$ h vud fHklu n[kh g; I Hkh fHklu ifjes I ;k, j gksh g; D; k vki bl dk dkj.k crk l drsg; n'keyo I ;k vka0-5] 2-3] 0-333 bR; kfn o; ckjs e;D; k dgk tk l drk g; bl i dkj dh i R; d I ;k dks, d l kekU; fHklu o; : i e; fy[kk tk l drk g; vks bl hfy, ; si fjes I ;k, j g; mnkgj.kkFkj 0.5 = $\frac{5}{10}$, 2.3 = $\frac{23}{10}$,

$$0.333 = \frac{333}{1000} \text{ bR; kfnA}$$

iż kl dñft,

1. D;k | ፩; k $\frac{2}{63}$ ifjes | ፩; k gš bl oč ckjs eä lkp, A
2. nl ifjes | ፩; k vka dh , d lph cukb, A



vák vks gj

$\frac{p}{q}$ e] iwlkd p vák gsrFkk iwlkd q(0) gj gš

bl iżkij] $\frac{63}{7}$ e] 63 vák gš vks 7 gj gš

, dh ikp ifjes | ፩; k, i fyf[k,] ftueals iR; d dk

- (a) vák , d ½.kkRed iwlkd gks vks gj , d èkukRed iwlkd gš
- (b) vák , d èkukRed iwlkd gks vks gj , d ½.kkRed iwlkd gš
- (c) vák vks gj nkska ½.kkRed iwlkd gš
- (d) vák vks gj nkska èkukRed iwlkd gš

● D;k iwlkd Hkh ifjes | ፩; k, i gš

fdlh Hkh iwlkd dks , d ifjes | ፩; k ekuk tk ldrk gš mnkgj.kkFkj iwlkd 65 , d ifjes

| ፩; k gš D;k fd vki bls $\frac{65}{1}$ oQ : i eafy[k ldrk gš iwlkd o dks Hkh 0 $\frac{0}{2}$;k $\frac{0}{7}$

bR; kfn oQ : i eafy[k tk ldrk gš vr% ;g Hkh , d ifjes | ፩; k gš

bl iżkij] ifjes | ፩; k vka eä iwlkd vks fHku lfeefyr gks gš

ler; ifjes | ፩; k, i

, d ifjes | ፩; k dks vyx&vyx vákka vks gjakd iżkx djrs gq fy[k tk ldrk gš

mnkgj.kkFkj ifjes | ፩; k $\frac{62}{3}$ ij fopkj dñft , A

$$\frac{62}{3} = \frac{62 \times 2}{3 \times 2} - \frac{64}{6} A \text{ ge nEks gš fd } \frac{62}{3} \text{ ogh gš tks } \frac{64}{6} gš$$

$$I kFk gh] \frac{62}{3} = \frac{62 \times 65}{3 \times 65} - \frac{10}{615} gš vr% \frac{62}{3} \text{ ogh gš tks } \frac{10}{615} gš$$

$$bl iżkij] \frac{62}{3} = \frac{64}{6} = \frac{10}{15} gš , dh ifjes | ፩; k, i tks ijLij cjkj gš , d nlljs$$

oQ ler; (equivalent) ;k r; dgh tkrh gš



i 4%

$$\frac{10}{-15} = \frac{-10}{15} \text{ (diss)}$$

i 7 kl dhft,

fjDr LFkkuk dks Hkfj, %

(i) $\frac{5}{4}$ $\frac{\square}{16}$ $\frac{25}{\square}$ $\frac{615}{\square}$

(ii) $\frac{63}{7}$ $\frac{\square}{14}$ $\frac{9}{\square}$ $\frac{66}{\square}$

, d ifjes I 7; k o v k v k g j dks, d gh 'k; rj (non-zero) i wkked ls xqkk djus ij] ge a nh g p i fjes I 7; k o v k v k g j ; , d v u; ifjes I 7; k i k l r g k s h g ; g Bhd Lery; fHkku i k l r djus t s k gh g ; xqkk d h rjgj , d gh 'k; rj i wkked ls v k v k v k g j dks Hkx nus ij Hkh Lery; ifjes I 7; k, i k l r g k s h g ; mnkgj. k k Fk]

$$\frac{10}{615} = \frac{10}{615} \frac{65}{65} \frac{62}{3}, \quad \frac{612}{24} = \frac{612}{24} \frac{12}{12} \frac{61}{2}$$

$$\text{ge } -\frac{2}{3} \text{ dks} - \frac{2}{3}, -\frac{10}{15} \text{ dks} - \frac{10}{15} \text{ bR; kfn} \text{ fy[krs g]}$$

9.4 èkukRed v k ½. kkRed i fjes I 7; k, i

i fjes I 7; k $\frac{2}{3}$ ij fopkj dhft, A bl I 7; k o v k v k g j nksa gh èkukRed i wkked g;

, s h i fjes I 7; k dks, d èkukRed i fjes I 7; k dgrsg; vr% $\frac{3}{8}, \frac{5}{7}, \frac{2}{9}$ bR; kfn èkukRed i fjes I 7; k, i g;

i 7 kl dhft,

- D;k 5 , d èkukRed i fjes I 7; k g;
- i k p v k èkukRed i fjes I 7; k, i fyf[k, A

$\frac{63}{5}$ dk v k , d ½. kkRed i wkked g; tcfd bl dk g j , d èkukRed i wkked g; , s h i fjes I 7; k dks ½. kkRed i fjes I 7; k dgrs g; vr% $\frac{65}{7}, \frac{63}{8}, \frac{69}{5}$ bR; kfn ½. kkRed i fjes I 7; k, i g;

i 7 kl dhft,

- D;k & , d ½. kkRed i fjes I 7; k g;
- i k p v k ½. kkRed i fjes I 7; k, i fyf[k, A

• D;k $\frac{8}{3}$, d ½. kkRed I 7; k g; ge tkurs g; fd $\frac{8}{3} = \frac{8(-1)}{-3(-1)} = \frac{8}{3}$

g; rFkk $\frac{8}{3}$, d ½. kkRed i fjes I 7; k g; vr% $\frac{8}{3}$, d ½. kkRed i fjes I 7; k g;

bl h i dkj] $\frac{5}{67}, \frac{6}{65}, \frac{2}{69}$ bR; kfn I Hkh ½. kkRed i fjes I 7; k, i g; è; ku nlft, fd buo v k èkukRed g; rFkk g; ½. kkRed g;

• I 7; k 0 u rks , d èkukRed i fjes I 7; k g; v k u gh , d ½. kkRed i fjes I 7; kA

• $\frac{63}{65}$ o ckjs ea D;k dgk tk I drk g;

vki ns~~kks~~ fd $\frac{63}{65}$ $\frac{63}{65}$ (61) $\frac{3}{5}$ g~~a~~ vr% $\frac{63}{65}$, d èkukRed ifjes $I\ddot{a};k$ g~~a~~ bl
i~~dkj~~ $\frac{62}{65}, \frac{65}{63}$, bR; kfn èkukRed ifjes $I\ddot{a};k,i$ g~~a~~



i~~z~~ kl dhft,

fuEufyf[kr ea ls ck~~s&l~~ h $I\ddot{a};k,i$ ½.kkRed ifjes $I\ddot{a};k,i$ g~~a~~

- | | | | | | |
|--------------------|--------------------|----------------------|--------|--------------------|----------------------|
| (i) $\frac{62}{3}$ | (ii) $\frac{5}{7}$ | (iii) $\frac{3}{65}$ | (iv) 0 | (v) $\frac{6}{11}$ | (vi) $\frac{62}{69}$ |
|--------------------|--------------------|----------------------|--------|--------------------|----------------------|



9.5 , d $I\ddot{a};k,j\ddot{k} i j$ ifjes $I\ddot{a};k,i$

vki ;g tkurs~~g~~ fd ,d $I\ddot{a};k,j\ddot{k} i j$ i~~wkkel~~ adksfdl i~~dkj~~ fu: fir fd;k tkrk g~~a~~ vkb,
,~~h~~ gh ,d $I\ddot{a};k,j\ddot{k} [kpo]$



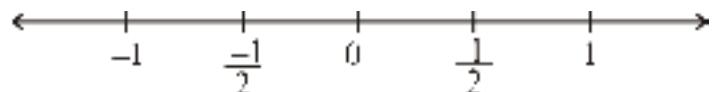
0 o~~l~~ nkb±v~~kj~~ o~~l~~ cnv~~k~~ adks + fpÉ l~~s~~ 0; Dr djrs g~~a~~ v~~kj~~; sèkukRed i~~wkkel~~ n'kk~~s~~ g~~a~~
0 ls ckb±v~~kj~~ o~~l~~ cnv~~k~~ adks ó fpÉ l~~s~~ 0; Dr djrs g~~a~~ v~~kj~~; s ½.kkRed i~~wkkel~~ n'kk~~s~~ g~~a~~
 $I\ddot{a};k,j\ddot{k} i j$ fHklu~~k~~ o~~l~~ fu: i.k ls Hkh vki ifjfpr g~~a~~
vkb, vc ns~~k~~ fd ifjes $I\ddot{a};k,i$ $I\ddot{a};k,j\ddot{k} i j$ fd l i~~dkj~~ fu: fir dh tk ldrh g~~a~~
vkb, $I\ddot{a};k,j\ddot{k} i j$ $I\ddot{a};k,i$ $\frac{1}{2}$ adks fu: fir dj~~a~~

t~~s~~ k fd /ukRed i~~wkkel~~ adh fLFkfr eaf~~d~~;k x;k Fkk] èkukRed ifjes $I\ddot{a};kvk$ adks 0
o~~l~~ nkb±v~~kj~~ v~~fdr~~ fd;k tk, xk rFkk ½.kkRed ifjes $I\ddot{a};kvk$ adks 0 o~~l~~ ckb±v~~kj~~ v~~fdr~~
fd;k tk, xkA

0 o~~l~~ fd l v~~kj~~ vki $\frac{1}{2}$ adks v~~fdr~~ dj~~a~~ ½.kkRed ifjes $I\ddot{a};k$ g~~ks~~ o~~l~~ dkj.k bl s
0 o~~l~~ ckb±v~~kj~~ v~~fdr~~ fd;k tk, xkA
vki tkursg~~g~~ fd $I\ddot{a};k,j\ddot{k} i j$ i~~wkkel~~ adks v~~fdr~~ djrs l e;] m~~ukj~~ k~~j~~ i~~wkkel~~ adks l eku
vrjk~~yk~~ i j v~~fdr~~ fd;k tkrk g~~a~~ l kFk gh] $I\ddot{a};kvk$ 1 v~~kj~~ &1 dk ;je $I\ddot{a};k$ 0 ls enyLFk
g~~a~~ bl h i~~dkj~~] 2 v~~kj~~ 62 rFkk 3 v~~kj~~ 63 Hkh l enyLFk g~~a~~

b~~l~~ h i~~dkj~~] ifjes $I\ddot{a};k,i$ $\frac{1}{2}$ v~~kj~~ $\frac{1}{2}$ Hkh 0 ls enyLFk g~~ks~~ ge tkursg~~g~~ fd ifjes
 $I\ddot{a};k$ $\frac{1}{2}$ adks fd l i~~dkj~~ $I\ddot{a};k,j\ddot{k} i j$ v~~fdr~~ fd;k tkrk g~~a~~; g ml cnqij v~~fdr~~ fd;k

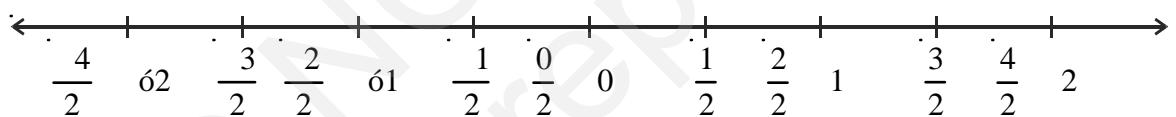
tkrk ḡ tks 0 v̄k̄ 1 ls cjkj nj̄ (Bhd chp e) ij ḡ v̄Fk̄~0 v̄k̄ 1 dh v̄k̄eh nj̄
ij ḡ bl fy,] $\frac{1}{2}$ dks 0 v̄k̄ 61 dh v̄k̄eh nj̄ ij v̄fdr fd;k tk,xkA



ge tkurs ḡ fd $\frac{3}{2}$ dks l; k j; k ij fdl idkj v̄fdr fd;k tkrk ḡ bl s 0 o; nk̄±
v̄k̄ 1 v̄k̄ 2 o; chp e v̄k̄eh nj̄ ij v̄fdr fd;k tkrk ḡ v̄k̄, vc l; k j; k ij $\frac{3}{2}$
dks v̄fdr dj; g 0 o; ck̄±v̄k̄ mruh gh nj̄ ij v̄fdr ḡk̄ ftruh nj̄ 0 v̄k̄ $\frac{3}{2}$ o;
chp ḡ

?Vrs ḡ Øe ea $\frac{-1}{2}, \frac{-2}{2}$ ($= -1$), $\frac{3}{2}, \frac{4}{2}$ (-2), bR; kfn i; k r ḡ bl l; g inf'kr

ḡk̄k ḡ fd $\frac{3}{2}$ l; k v̄k̄o 1 v̄k̄ 62 o; chp e v̄k̄eh nj̄ ij fLkr (; k v̄fdr) ḡk̄kA



bl h idkj] $\frac{5}{2}$ v̄k̄ $\frac{7}{2}$ dks l; k j; k ij v̄fdr dhft,A

bl h idkj] $\frac{1}{3}$ l; k j; k ij 0 o; ck̄±v̄k̄ 'k; l smruh gh nj̄ ij ḡk̄ ftruh fd
 $\frac{1}{3}$ 'k; ls nk̄±v̄k̄ ḡ

v̄r% t; k fd Åij fd;k x;k ḡ $\frac{1}{3}$ dks l; k j; k ij fu: fir fd;k tk l drk ḡ , d
ckj] gea $\frac{1}{3}$ dks l; k j; k ij fu: fir djuk v̄k tk, rk̄ ge $\frac{2}{3}, \frac{4}{3}, \frac{5}{3}, \dots$ bR; kfn
dks l; k j; k ij fu: fir dj l drs ḡ fo; fHklu gj; k; okyh v̄l; ifjes l; k v̄k̄ dks Hk h bl h
idkj l; k j; k ij fu: fir fd;k tk l drk ḡ

9.6 ekud : i eifjes l; k, j

fuEufyf[kr ifjes l; k v̄k̄ dks nf[k, %

$$\frac{3}{5}, \frac{5}{8}, \frac{2}{7}, \frac{7}{11}$$



bu lHkk ifjes l{:kvka@ gj ekukRed iwkkel g@rFkk v@k v@j gjka@ chp eao@ 1
 lkozqku [common factor] g@ l kFk gh] ½.kRed fpE (&) oao@ v@k eagh fLFkr g@
 , d h ifjes l{:kvka dksekud : i (standard form) eao@ Dr dh xbz ifjes l{:k, i
 dgk tkrk g@

, d ifjes l^g;k ekud : i e¹0;Dr dh g^hz dgh tkrh g^h ;fn ml dk gj èkukRed
i wkkd gks rFkk ml oQ v^hk v^hg gj e¹ oQ vfrfjDr dk^hz l koZ xqku[kM u g^hk

;fn dkBz ifjes l^ä;k ekud : i e^äughag^ä rks ml s ml o^ä ekud : i e^ä0;Dr fd;k tk l drk g^ä

Lej.k dhft, fd fHkkukadks muoꝝ U; ure : i ka ea 0; Dr djus oꝝ fy,] geus muoꝝ vā kka
vks gjk adks, d gh 'kH; sj i wkked l s Hkkx fn;k FkkA ge bl h fofek dk i z kx ifjes l {; kvka
adks muoꝝ ekud : i ka ea 0; Dr djus ea djksA

mngj.k 1 $\frac{645}{30}$ dks ekud : i e@0; Dr dhft, A

gy	geɪ̯ iklr g%	$\frac{645}{30}$	$\frac{645}{30} \quad 3$	$\frac{615}{10}$	$\frac{615}{10} \quad 5$	$\frac{63}{2}$
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geanksckj Hkkx nsik iMIA igyh ckj 3 lsvk§ fi0j 5 lA blsfuEufyf[kr idkj lsHkh
fd;k tk ldrk Fkk %

$$\begin{array}{r} \overset{6}{4}5 \\ 30 \end{array} \quad \begin{array}{r} \overset{6}{4}5 & 15 \\ 30 & 15 \end{array} \quad \begin{array}{r} 63 \\ 2 \end{array}$$

bl mnkgj.k eə nʃ[k, fd 15] l ɿ;kvkə 45 vks 30 dk e-l - ga

bl i dkj], d ifjes l[; k dksekud : i ea 0; Dr djus o fy,] ge ml o v k v k
gj dksmuo e-l - l} ½.k fpÉ ij fcuk dkbz è; ku fn, (; fn dkbz gk) Hkkx ns s g (½.k
fpÉ ij è; ku uk ns s dk dkj.k ge vxyl d{kkvka ea i <s>
; fn gj ea ½.kkRed fpÉ gs rks ^&e-l - * l s Hkkx nhft, A

mnkgj.k 2 ekud : i eacnfy, %

$$\text{(i)} \quad \frac{36}{624} \qquad \qquad \text{(ii)} \quad \frac{63}{615}$$

gy

- (i) 36 vks 24 dk e-l- 12 gj
vr% ekud : i vks vks gj dks 612 l s Hkkx nus ij iklr gksxKA

$$\text{bl} \quad i \text{d}k\text{j] } \frac{36}{624} \quad \frac{36}{624} \frac{(612)}{(612)} \quad \frac{3}{2}$$

- (ii) 3 vks 15 dk e-l - 3 g

$$bl \quad i \boxed{dkj} \quad \frac{63}{615} \quad \frac{63}{615} \quad \frac{(63)}{(63)} \quad \frac{1}{5}$$





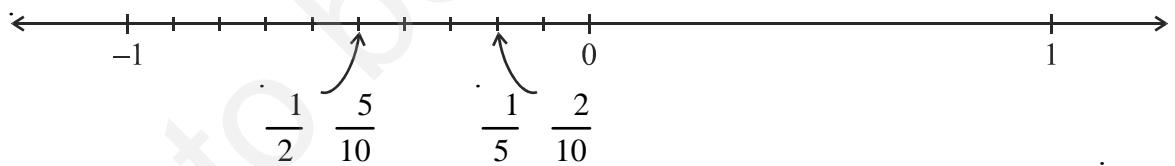
i_z kl dhft,

ekud : i Kkr dhft, (i) $\frac{618}{45}$ (ii) $\frac{612}{18}$

9.7 ifjes I_z; kvkadh ryuk

ge ;g tkurs g_z fd nks i wkkedka ; k nks fHkuka dh ryuk fd l i_z k j dh tkrh gSrFkk ; g Hkh fd bueadk_z CM_z gSv_z dks Nk_zKA vkb, vc n_z fd nks ifjes I_z; kvkadh ryuk fd l i_z k j dh tk l drh g_z

- $\frac{2}{3} v_{kz} \frac{5}{7} t_{sh}$ nks ekukRed ifjes I_z; kvkadh ryuk Bhd ml h i_z k j dh tk l drh g_z t_{sh} fd ge fHkuka dh fLFkr o_z fy, igysi <+p_z g_z
- ejh usnks 1/2. k Red ifjes I_z; kvkadh ryuk $I_{z} = \frac{1}{2} v_{kz} - \frac{1}{5}$ dh ryuk I_z; k j_z dk i_z kx djrs g_z dh ml s Kkr Fkk fd nks i wkkedka e_z og i wkked CM_z Fkk tks n_z js i wkked o_z nkb±v_z fLFkr Fkk
mnkgj.kkFk] I_z; k j_z i_z i wkked 5 i wkked 2 o_z nkb±v_z fLFkr gSrFkk 5 > 2 g_z I_z; k j_z i_z i wkked μ2 i wkked μ5 o_z nkb±v_z fLFkr gSrFkk 62 > 65 g_z
ml us bl fofek dk i_z kx ifjes I_z; kvkadh ryuk, Hkh fd; kA ml sirk Fkk fd I_z; k j_z k i_z ifjes I_z; kvkadh fd l i_z k j_z v_z dr (fu: fir) fd; k tkrk g_z ml us - $\frac{1}{2} v_{kz}$
 $\frac{1}{5}$ dks uhp_z n'kz vud k j v_z dr fd; k%



D; k ml us nks a_z cny_z l gh i_z k j l sv_z dr fd, g_z ml us d_z s v_z D; k a - $\frac{1}{2}$ dks $\frac{5}{10}$

rFkk $\frac{1}{5}$ dks $\frac{2}{10}$ e_z cny_z ml s Kkr g_z k fd ifjes I_z; k $\frac{1}{5}$ ifjes I_z; k - $\frac{1}{2}$ o_z nkb±v_z fLFkr g_z bl i_z k j $\frac{1}{5} > -\frac{1}{2}$ g_z; k $-\frac{1}{2} < \frac{1}{5}$ g_z

D; k vki $\frac{3}{4} v_{kz} - \frac{2}{3}$ dh rFkk $\frac{1}{3} v_{kz} - \frac{1}{5}$ dh ryuk dj l drs g_z

ge fHkuka o_z vius v_z; u l s ; g tkurs g_z fd $\frac{1}{5} < \frac{1}{2}$ g_z l kFk gh ejh us - $\frac{1}{2} v_{kz} - \frac{1}{5}$ o_z fy, D; k i_z k j fd; k A D; k ; g bl dk Bhd foijhr ugha FkkA

$$\text{vki nks gfd } \frac{1}{2} > \frac{1}{5} \text{ g} \quad \text{i jrq } \frac{1}{2} < \frac{1}{5} \text{ g}$$

$$D;k \text{ vki } \frac{3}{4} \text{ vki } \frac{2}{3} \text{ rFkk } \frac{1}{2} \text{ vki } \frac{1}{5} \text{ of fy, Hkh bl h i dklj dk ifj. kke nks g} \\ \text{ejh dks ;kn vkrk gfd ml us i wkkedka es i < Fkk fd } 4 > 3 \text{ g} \quad \text{i jrq } 4 < 63 \text{ g } 5 > 2 \text{ g} \quad \text{i jrq } 6 < 62 \text{ bR; kfnA}$$

- $\frac{1}{2}.$ kkRed ifjes | {; k vka of ; k vka dh fLFkfr Hkh Bhd bl h i dklj g nks $\frac{1}{2}.$ kkRed ifjes | {; k vka dh ryuk djus of fy,] ge mudh ryuk muo fpÉka dks NkMfs gq djrs g vki ckn es v fedk (inequality) of fpÉ dks mYVh dj (cny) nrs g mnkgj. k 7 vki 5 3 , dh ryuk djus of fy,] igysge 7 vki 5 3 dh ryuk djrs g ge 7 5 < 5 3 i klr gksk gsvki bl ls ge fu"d"k fudkyrs gfd 67 5 > 65 3 g dks cMk g % 3 8 ;k 2 7 ;k 4 3 ;k 3 2 ?

- d $\frac{1}{2}.$ kkRed vki èkukRed ifjes | {; k dh ryuk lti "V g | {; k jskk ij , d $\frac{1}{2}.$ kkRed ifjes | {; k 'k; of ckbo vki fLFkr gksr gsrFkk , d èkukRed ifjes | {; k 'k; of nkbo vki fLFkr gksr g vr% , d $\frac{1}{2}.$ kkRed ifjes | {; k lns , d èkukRed ifjes | {; k l s NkVh gksr g bl i dklj 6 2 < 1 2 g

- ifjes | {; k vka 3 vki 10 of chp es i wkl | {; k, i fxuuk pkgrh FkhA ml dks viuh fi Nyh d{k vka l s ;g Kkr Fkk fd 3 vki 10 of chp es Bhd 6 i wkl | {; k, i gksrh bl h i dklj] og µ3 vki 3 of chp i wkkedka dh | {; k Hkh Kkr djuk pkgrh FkhA µ3 vki 3 of chp es i wkkedka µ2] µ1] 0] 1 vki 2 g bl i dklj] µ3 vki 3 of chp Bhd 5 i wkked g

9.8 nks i fjes | {; k vka of chp es i fjes | {; k, i

jsek 3 vki 10 of chp es i wkl | {; k, i fxuuk pkgrh FkhA ml dks viuh fi Nyh d{k vka l s ;g Kkr Fkk fd 3 vki 10 of chp es Bhd 6 i wkl | {; k, i gksrh bl h i dklj] og µ3 vki 3 of chp i wkkedka dh | {; k Hkh Kkr djuk pkgrh FkhA µ3 vki 3 of chp es i wkkedka µ2] µ1] 0] 1 vki 2 g bl i dklj] µ3 vki 3 of chp Bhd 5 i wkked g

D;k μ3 vks μ2 oč chp dkbz i wkked gk ugh μ3 vks μ2 oč chp dkbz i wkked ugha
gk nks Øekxr i wkked oč chp i wkked dh lq;k 0 gkrh gk
bl i ddkj] ge i klr djrs gfd nks i wkked oč chp ea i wkked dh lq;k lher ifjer ;k
(finite) gkrh gk
D;k ;g ifjes lq;kvka dh fLFkfr ea Hkh gksck\

jšek us nks ifjes lq;k, i $\frac{63}{5}$ and $\frac{61}{3}$ y\

ml us blg\ lku gj okyh ifjes lq;kvka ea cny fy;ka

vr% $\frac{63}{5} \frac{69}{15} \frac{61}{3} \frac{65}{15}$ gk

gea i klr gfd $\frac{69}{15} \frac{68}{15} \frac{67}{15} \frac{66}{15} \frac{65}{15}$ g; k $\frac{63}{5} \frac{68}{15} \frac{67}{15}$ $\frac{66}{15} \frac{61}{3}$ gk

bl i ddkj] og $\frac{3}{5}$ vks $\frac{1}{3}$ oč chp ea ifjes lq;k, i $\frac{68}{15}, \frac{67}{15}, \frac{66}{15}$ Kkr dj ldm\

D;k $\frac{-3}{5}$ vks $\frac{-1}{3}$ oč chp ea ooy ifjes lq;k, i $\frac{68}{15}, \frac{67}{15}, \frac{66}{15}$ gh gk

gea i klr gfd $\frac{63}{5} \frac{618}{30} \frac{618}{15} \frac{68}{15} \frac{616}{30}$ gk

l kfk gh] $\frac{618}{30} \frac{617}{30} \frac{616}{30}$ gk vFkk\ - $\frac{63}{5} \frac{617}{30} \frac{68}{15}$ gk

vr% $\frac{63}{5} \frac{617}{30} \frac{68}{15} \frac{67}{15} \frac{66}{15} \frac{61}{3}$ gk

bl i ddkj] $\frac{-1}{3}$ vks $\frac{-3}{5}$ oč chp ge ,d vks ifjes lq;k Kkr djus ea l i ly gks x,A

bl fofek dk i zks djo\ vki nks ifjes lq;kvka oč chp ea ftruh pkgs mruh ifjes
lq;k, i Kkr dj l drs gk

mnkgj.kkfk] $\frac{63}{5} \frac{63}{5} \frac{30}{30} \frac{690}{150} vks \frac{61}{3} \frac{61}{3} \frac{50}{50} \frac{650}{150}$ gk

gea $\frac{-90}{150}$ vks $\frac{-50}{150}$ oč chp ea vFkk\ - $\frac{-3}{5}$ vks $\frac{-1}{3}$ oč chp ea 39

ifjes lq;k, i $\frac{89}{150}, \frac{88}{150}, \frac{87}{150}, \dots, \frac{51}{150}$ i klr djrs gk

vki ;g Kkr djks fd ;g lph dHkh leklr ugha gksck\

D;k vki $\frac{-5}{3}$ vks $\frac{-8}{7}$ oč chp ea ikp ifjes lq;k, i fy[k l drs gk

ge nks ifjes lq;kvka oč chp ea vIher (;k vifjer : i ls vud)
ifjes lq;k, i Kkr dj l drs gk



i z kl dhft,

$\frac{-5}{7}$ vks $\frac{-3}{8}$ oč chp ea
ikp ifjes lq;k, i Kkr
dhft,A

mnkgj.k 4 ፦ ፲ vks ፦ ፧ oč chp eårhu ifjes | ፩; k, i fyf[k, A

gy vkb, ፦ ፧ ፦ ፧ dks gj ጀ okyh ifjes | ፩; k, i vks oč : i ea fy [kA

gea iklr gsf fd ፦ ፧ = $\frac{5}{5}$ vks ፦ ፧ = $\frac{10}{5}$ gA

vr% $\frac{610}{5} \frac{69}{5} \frac{68}{5} \frac{67}{5} \frac{66}{5} \frac{65}{5}$ g ; k ፦ ፧ $\frac{69}{5} \frac{68}{5} \frac{67}{5} \frac{66}{5}$ ፦ ፧ gA

62 vks ፦ ፧ oč chp rhu ifjes | ፩; k, i $\frac{9}{5}, \frac{8}{5}, \frac{7}{5}$ gkxhA

(vki $\frac{69}{5}, \frac{68}{5}, \frac{67}{5}$ vks $\frac{-6}{5}$ ea ls dkbz lh Hkh rhu ifjes | ፩; k, i ys l drs gA)

mnkgj.k 5 fuEufyf[kr ifr: i (Pattern) ei pkj vks | ፩; k, i fyf[k, %

$$\frac{-1}{3}, \frac{-2}{6}, \frac{-3}{9}, \frac{-4}{12}, \dots$$

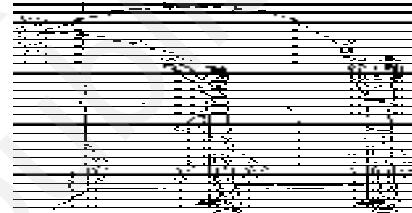
gy gea iklr g%

$$\frac{2}{6} \frac{1}{3} \frac{2}{2}, \frac{3}{9} \frac{1}{3} \frac{3}{3}, \frac{4}{12} \frac{1}{3} \frac{4}{4}$$

vFlok $\frac{61}{3} \frac{1}{1} \frac{1}{3}, \frac{61}{3} \frac{2}{2} \frac{62}{6}, \frac{61}{3} \frac{3}{3} \frac{63}{9}, \frac{61}{3} \frac{4}{4} \frac{64}{12}$ gA

bl i dkj] bu | ፩; k, i vks e a ge , d ifr: i nks gA

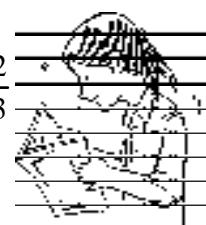
vll; | ፩; k, i $\frac{1}{3} \frac{5}{5} \frac{5}{15}, \frac{1}{3} \frac{6}{6} \frac{6}{18}, \frac{1}{3} \frac{7}{7} \frac{7}{21}$ gkxhA



izukoyh 9.1

1. fuEufyf[kr ifjes | ፩; k, i vks oč chp e a ikp ifjes | ፩; k, i fyf[k, %

$$(i) \quad ፦ ፧ 0 \quad (ii) \quad ፦ ፧ ፦ ፧ \quad (iii) \quad \frac{-4}{5} vks \frac{-2}{3} \quad (iv) \quad -\frac{1}{2} vks \frac{2}{3}$$



2. fuEufyf[kr ifr: ikaea ls iR; d e a pkj vks ifjes | ፩; k, i fyf[k, %

$$(i) \quad \frac{3}{5}, \frac{6}{10}, \frac{9}{15}, \frac{12}{20}, \dots \quad (ii) \quad \frac{1}{4}, \frac{2}{8}, \frac{3}{12}, \dots$$

$$(iii) \quad \frac{1}{6}, \frac{2}{12}, \frac{3}{18}, \frac{4}{24}, \dots \quad (iv) \quad \frac{2}{3}, \frac{2}{3}, \frac{4}{6}, \frac{6}{9}, \dots$$

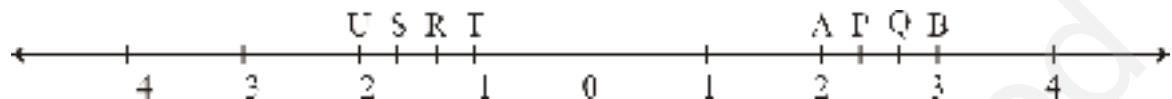
3. fuEufyf[kr oč lerY; pkj ifjes | ፩; k, i fyf[k, %

$$(i) \quad \frac{2}{7} \quad (ii) \quad \frac{5}{3} \quad (iii) \quad \frac{4}{9}$$

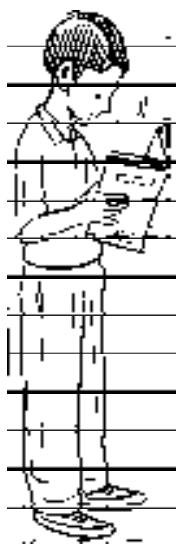
4. , d l ; k j ; kk [k]p, v k m i j fuEufyf[kr i fjes l ; k v k dks fu: fir dhft, %

- (i) $\frac{3}{4}$ (ii) $\frac{5}{8}$ (iii) $\frac{7}{4}$ (iv) $\frac{7}{8}$

5. , d l ; k j ; kk i j c n q P, Q, R, S, T, U, A v k B b l i d k j g fd TR = RS = SU
r F k AP = PQ = QB g P, Q, R v k s l s fu: fir i fjes l ; k v k dks fyf[k, A



6. fuEufyf[kr e a l s d k & l s ; l e , d g h i fjes l ; k dks fu: fir djrs g



- (i) $\frac{7}{21}$ v k $\frac{3}{9}$ (ii) $\frac{16}{20}$ v k $\frac{20}{25}$ (iii) $\frac{2}{3}$ v k $\frac{2}{3}$
(iv) $\frac{3}{5}$ v k $\frac{12}{20}$ (v) $\frac{8}{5}$ v k $\frac{24}{15}$ (vi) $\frac{1}{3}$ v k $\frac{1}{9}$
(vii) $\frac{5}{9}$ v k $\frac{5}{9}$

7. fuEufyf[kr i fjes l ; k v k dks mu o l j y r e : i e a f y f [k, %

- (i) $\frac{8}{6}$ (ii) $\frac{25}{45}$ (iii) $\frac{44}{72}$ (iv) $\frac{8}{10}$

8. l o r k a >, <, v k = e a l s l g h l o r p y d j f j D r L F k k u d k s H k f j , %

- (i) $\frac{5}{7} \boxed{\quad} \frac{2}{3}$ (ii) $\frac{4}{5} \boxed{\quad} \frac{5}{7}$ (iii) $\frac{7}{8} \boxed{\quad} \frac{14}{16}$
(iv) $\frac{8}{5} \boxed{\quad} \frac{7}{4}$ (v) $\frac{1}{3} \boxed{\quad} \frac{1}{4}$ (vi) $\frac{5}{11} \boxed{\quad} \frac{5}{11}$
(vii) $0 \boxed{\quad} \frac{7}{6}$

9. fuEufyf[kr e a i ; d e a l s d k & l h l ; k c M h g

- (i) $\frac{2}{3}, \frac{5}{2}$ (ii) $\frac{5}{6}, \frac{4}{3}$ (iii) $\frac{3}{4}, \frac{2}{3}$
(iv) $\frac{1}{4}, \frac{1}{4}$ (v) $3\frac{2}{7}, 3\frac{4}{5}$

10. fuEufyf[kr i fjes l ; k v k dks v k j k g h Øe e a f y f [k, %

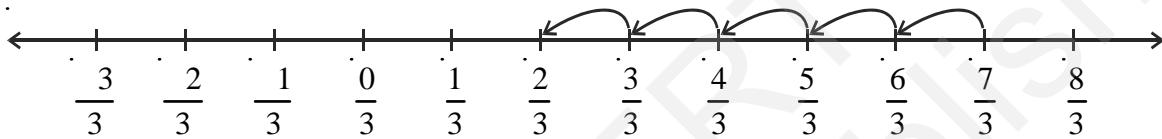
- (i) $\frac{3}{5}, \frac{2}{5}, \frac{1}{5}$ (ii) $\frac{61}{3}, \frac{2}{9}, \frac{4}{3}$ (iii) $\frac{3}{7}, \frac{3}{2}, \frac{3}{4}$

9.9 ifjes $I\ddot{e};kv\ddot{a}ij$ $I\ddot{e}\emptyset;k,j$

Vki tkursg \ddot{s} fd i wkkelkarFkk fHkkuka dksfdl izdkj tkm \ddot{a} ?kvk;k] xqkk vks Hkkx fd;k tkrk g \ddot{s} vkb, bu vkekjkHkk \ddot{a} $I\ddot{e}\emptyset;kv\ddot{a}dk$ ifjes $I\ddot{e};kv\ddot{a}ij$ v $\ddot{e};;u$ dj \ddot{a}

9.9.1 ;ks

- vkb, leku gj okyh nks ifjes $I\ddot{e};kv\ddot{a}ij$ leku yift, $\frac{7}{3}$ vks $\frac{5}{3}$] dks tkm \ddot{a} ge $\frac{7}{3}$ $\frac{5}{3}$ Kkr djrs g \ddot{s} $I\ddot{e};k j\ddot{e}kk ij$ ges iklr gksk g \ddot{s} %

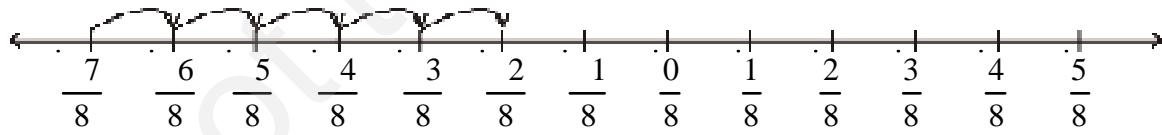
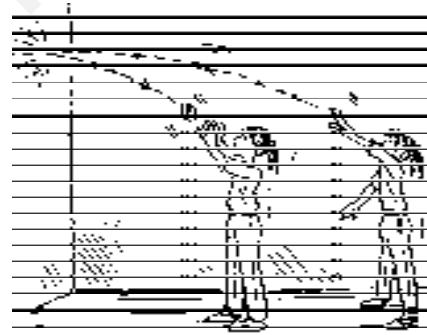


nks Øekxr cnykaof chp dh nj \ddot{a} $\frac{1}{3}$ g \ddot{s} vr% $\frac{7}{3}$ e \ddot{s} $\frac{5}{3}$ tkmusdk vFkz g \ddot{s} fd $\frac{7}{3}$ ol
ckb±vks 5 dne py \ddot{a} ge dgk \ddot{a} igprsg \ddot{s} ge $\frac{2}{3}$ ij igprsg \ddot{s} vr% $\frac{7}{3}$ $\frac{5}{3}$ $\frac{2}{3}$ g \ddot{s}
vkb, bl dks bl izdkj djus dk izru dj \ddot{a} %

$$\frac{7}{3}, \frac{5}{3}, \frac{7}{3}, \frac{5}{3}, \frac{2}{3}$$

ges ogh m \ddot{u} kj iklr gksk g \ddot{s}

$\frac{6}{5}, \frac{2}{5}, \frac{3}{7}, \frac{5}{7}$ dks mijkDr nkskafofek; ka ls Kkr
dhft, vks tko dj \ddot{a} fd D;k nkska m \ddot{u} kj leku g \ddot{s}
bl h izdkj] $\frac{7}{8}, \frac{5}{8}$ fuEufyf[kr gksk %



ges D;k iklr gksk g \ddot{s}

I kFk gh] $\frac{7}{8}, \frac{5}{8}, \frac{7}{8}$? D;k nkska leku g \ddot{s}

izkl dhft,

$$\frac{13}{7}, \frac{6}{7}, rFkk \frac{19}{5}, \frac{7}{5} Kkr dhft, %$$



bl i₁dkj] ge n₁krs g₁fd l₁ku gj oky₁ ifjes l₁;kvka dks tkmf₁s l₁e;] ge] gj dks og₁ j[krs g₁] v₁l₁ka dks tkmf₁+nss g₁

$$bl i_1dkj] \frac{11}{5} \frac{7}{5} \frac{11}{5} \frac{7}{5} \frac{4}{5} g\ddot{a}$$

- ge vyx&vyx gj₁oky₁ nks ifjes l₁;kvka dks fd l₁dkj tkmf₁ f₁h₁l₁ukad₁ rjg₁] ge i₁gys bu gj₁ dk y-l₁- Kkr djrs g₁ fi₁g₁ ge ,d h l₁er₁; ifjes l₁;k₁ Kkr djrs g₁ ftuo₁ gj ;g y-l₁- g₁ bl o₁ ckn ge bu n₁kska ifjes l₁;kvka dks tkmf₁s g₁

$$mnkgj.j.kFk \frac{7}{5} \frac{2}{3} dks tkmf_1 5 vks 3 dk y-l-15 g\ddot{a}$$

$$vr\% \frac{7}{5} \frac{21}{15} vks \frac{2}{3} \frac{10}{15} g\ddot{a}$$

$$bl i_1dkj] \frac{7}{5} \frac{2}{3} \frac{21}{15} \frac{10}{15} \frac{31}{15} g\ddot{a}vka$$

; k₁; ifryke %

$$\frac{4}{7} \frac{4}{7} fdlo₁ cjkcj g₁sk\$$

$$\frac{4}{7} \frac{4}{7} \frac{4}{7} 0 g\ddot{a} l₁Fk gh] \frac{4}{7} \frac{4}{7} 0 g\ddot{a}$$

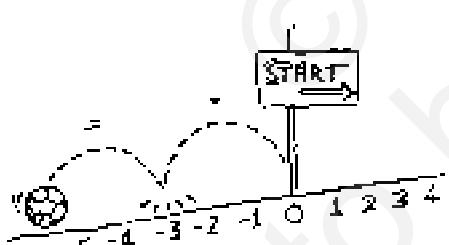
$$bl h i_1dkj] \frac{2}{3} \frac{2}{3} 0 \frac{2}{3} \frac{2}{3} g\ddot{a}$$

i₁z kl dhft,

Kkr dhft, %

$$(i) \frac{3}{7} \frac{2}{3}$$

$$(ii) \frac{5}{6} \frac{3}{11}$$



v₁l₁dk₁s, ln g₁skfd i₁l₁l₁ek₁ 2 dk ; k₁; ifryke (additive inverse) 2 g₁ rFk 2] i₁l₁l₁ek₁ 6 2 dk ; k₁; ifryke g₁sk₁ g₁

ifjes l₁;kvka o₁ fy₁] ge dgrs g₁fd $\frac{4}{7}$ ifjes l₁;k₁ $\frac{4}{7}$

dk ; k₁; ifryke g₁sk₁ $\frac{4}{7}$ ifjes l₁;k₁ $\frac{4}{7}$ dk ; k₁; ifryke g₁

bl h i_1dkj] $\frac{2}{3}$ ifjes l₁;k₁ $\frac{2}{3}$ dk ; k₁; ifryke g₁sk₁ $\frac{2}{3}$ ifjes

l₁;k₁ $\frac{2}{3}$ dk ; k₁; ifryke g₁

mnkgj.j.6 Ir₁ky fd l₁h LFku P l₁s i₁o₁ fn'kk e₁ $\frac{2}{3}$ km

pyrk g₁svks fi₁g₁ og₁ l₁sif₁ pe fn'kk e₁ $\frac{5}{7}$ km

pyrk g₁ vc og P l₁s dgk₁ fLFkr g₁sk\

i₁z kl dhft,

$$-\frac{3}{9}, -\frac{9}{11} vks \frac{5}{7} o\ddot{a}$$

; k₁; ifryke D; k g₁

gy vkb, i₁o₁z fn'kk e₁pyh xb₁njh dks ekukRed fpE l₁0;Dr dj₁ bl fy₁] if'pe fn'kk e₁pyh xb₁njh dks 1/2.kkRed fpE l₁0;Dr fd;k tk, xka

bl i²dkj] cnq P ls iriky dh njh (km e) g² %

$$\begin{aligned} \frac{2}{3} + 1\frac{5}{7} &= \frac{2}{3} + \frac{12}{7} = \frac{2}{3} + \frac{7}{7} = \frac{6}{7} + \frac{3}{7} \\ &= \frac{14}{21} + \frac{36}{21} = \frac{22}{21} = 1\frac{1}{21} \end{aligned}$$

D; k d ; g ½. k Red g² bl fy, Iriky P ls if'pe dh v² 1¹₂₁ km dh njh ij g²

9.9.2 0; odyu (?Vuk)

I fork us nks ifjes 1st; kvka $\frac{5}{7}$ v² $\frac{3}{8}$ dk vrj bl fofek ls ikkr fd;k %

$$\frac{5}{7} - \frac{3}{8} = \frac{40}{56} - \frac{21}{56} = \frac{19}{56}$$

i 0jhk tkurh Fkh fd nks i wkkdka v² b o² fy,] a² b = a + (b) fy [k tk l drk g²

ml us, d k ifjes 1st; kvka o² fy, Hkh fd;k v² Kkr fd;k fd $\frac{5}{7} - \frac{3}{8} = \frac{5}{7} + \frac{(-3)}{8} = \frac{19}{56}$ g²

nksuka us, d gh (I ek) vrj ikkr fd;kA

nksuka fofek; ka I } $\frac{7}{8} - \frac{5}{9}, \frac{3}{11} - \frac{8}{7}$ Kkr djusdk i²ru dlft, A D; k vki dks I ek m²ukj ikkr g²rs g²

vr% ge dgrs g²fd nks ifjes 1st; kvka dks ?Vkr (0; odyu djr) I e;] ?Vk, tkus okyh Ist; k o²; k; ifryke dks vU; ifjes 1st; k ea tkm+nuk pkfg, A

bl i²dkj, $1\frac{2}{3} - 2\frac{4}{5} = \frac{5}{3} - \frac{14}{5} = \frac{5}{3} + \frac{14}{5}$ dk ; k; ifryke

$$= \frac{5}{3} + \frac{(-14)}{5} = \frac{17}{15} = 1\frac{2}{15} g^2$$

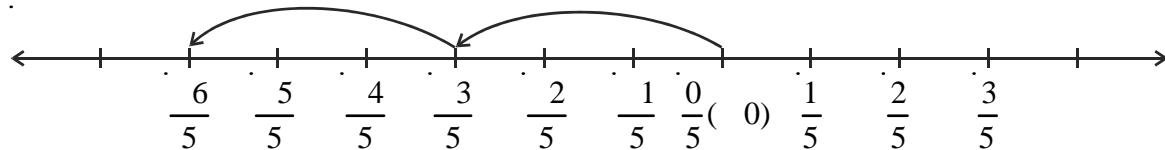
$\frac{2}{7} - \frac{5}{6}$ D; k g²sk\ $\frac{2}{7} - \frac{5}{6} = \frac{2}{7} - \frac{5}{6}$ dk ; k; ifryke

$$\frac{2}{7} - \frac{5}{6} = \frac{47}{42} - 1\frac{5}{42}$$

9.9.3 xqku

vkb, ifjes 1st; k $\frac{3}{5}$ dks2 ls xqkk dj² vFkk~ge $\frac{3}{5} \times 2$ Kkr dj²

Ist; k j²kk ij bl dk vFkZ g²sk $\frac{3}{5}$ fd ckb± v² nks dne pyukA



i² kl dlft,

Kkr dlft,

$$(i) \frac{7}{9} - \frac{2}{5} \quad (ii) 2\frac{1}{5} - \frac{1}{3}$$

ge dgk i gprsga ge $\frac{6}{5}$ ij i gprsga vkb, ge bl dks fHkkuka okyh fofek ls Kkr dj

$$\frac{3}{5} \times 2 = \frac{3 \times 2}{5} = \frac{6}{5}$$

ge ml h ifjes l; k ij i gpr tkrs ga

nkuka fofek; dk i zks djrs gq] $\frac{4}{7} \times 3$ vks $\frac{6}{5} \times 4$, dks Kkr dhft, A vki D; k nks gq

vr% ge Kkr djrs gfd, d ifjes l; k dks, d ekukRed i wkked ls xqkk djus ij

ge vkk dks ml i wkked ls xqkk dj nrs gsrFkk gj dks ogh j[krs gq

vkb, vc , d ifjes l; k dks, d 1/2. kRed i wkked ls xqkk dj

$$\frac{2}{9} \times (-5) = \frac{2 \times (-5)}{9} = \frac{10}{9}$$

i zkl dhft,

fuEufyf[kr xqkui ly D; k gks

$$(i) \frac{-3}{5}, 7 \quad (ii) \frac{-6}{5}, (-2)$$

; kn jf[k, fd 65 dks $\frac{5}{1}$ fy[kk tk ldrk ga

$$vr% \quad \frac{2}{9} \times \frac{5}{1} = \frac{10}{9} - \frac{2 \times 5}{9 \times 1} gq$$

$$bl h i dkj] \quad \frac{3}{11} \times (-2) = \frac{3 \times (-2)}{11 \times 1} = \frac{6}{11} gq$$

mijkDr i q.ka o vkkkj ij] ge Kkr djrs gfd $\frac{3}{8}, \frac{5}{7}, \frac{3}{8}, \frac{5}{7}, \frac{15}{56}$ gq

vr% tsk fd geusfHkkuka dh fLkrfr eafdf; k Fkk] ge nks ifjes l; kvk dks fuEufyf[kr fofek ls xqkk djrs gq

i zkl dhft,



Kkr dhft, %

$$(i) \frac{63}{4}, \frac{1}{7}$$

$$(ii) \frac{2}{3}, \frac{65}{9}$$

pj.k 1 % nks i fjes l; kvk o vakk dk xqkk dhft, A

pj.k 2 % nks i fjes l; kvk o gjk dk xqkk dhft, A

pj.k 3 % xqkui ly dks $\frac{pj.k 1 eikl ifj.kle}{pj.k 2 eikl ifj.kle}$ o : i eafyf[k, A

$$bl i dkj] \quad \frac{3}{5}, \frac{2}{7}, \frac{3}{5}, \frac{2}{7}, \frac{6}{35} gq$$

$$l kfk gh \quad \frac{-5}{8}, \frac{-9}{7} = \frac{(-5), (-9)}{8, 7} = \frac{45}{56} gq$$

9.9.4 foHkktu

fHkkuka o 0; 0 (reciprocals) o ckse ge igys i <+ppl gq $\frac{2}{7}$ dk 0; 0 e D; k gq

; g $\frac{7}{2}$ gq ge bl voekkj. lk dks ifjes l; kvk o 0; 0 e foy, Hkh ykxw djrs gq

bl i dkj] $\frac{2}{7}$ dk 0; 0 e $\frac{7}{2}$] vFkk ~ $\frac{7}{2}$ gksk rFkk $\frac{3}{5}$ dk 0; 0 e $\frac{5}{3}$ gkskA

ifjes 1{:k dk ml ds 0; Øe ls xqkui by
fdlh 1{:k dk ml o 0; Øe ls xqkui by lns 1 gksk g

$$\begin{aligned} \text{mnkgj.kfklz} &= \frac{4}{9} \times \left(\frac{4}{9} dk 0; Øe \right) \\ &= \frac{64}{9} \cdot \frac{69}{4} = 1 g \end{aligned}$$

$$\text{bl h idkj} \quad \frac{66}{13} \times \frac{613}{6} = 1 g$$

dn vks mnkgj.k yd] bl i{:k.k dh if"V dhft, A

I fork us, d ifjes 1{:k $\frac{4}{9}$ dks, d vll; ifjes 1{:k $\frac{5}{7}$ ls bl idkj foHkkftr fd;k
(Hkkx fn;k) %

$$\frac{4}{9} \quad \frac{5}{7} \quad \frac{4}{9} \quad \frac{7}{5} \quad \frac{28}{45}$$

ml us fHkkuka dh rjg gh 0; Øe dh voekkj.kk dk izks fd;k

vfi k us igys $\frac{4}{9}$ dks $\frac{5}{7}$ ls Hkkx fn;k vks $\frac{28}{45}$ ikr fd;k

vr e] ml us dgk fd $\frac{4}{9} \quad \frac{5}{7} \quad \frac{28}{45}$ g ml us, dk fdli idkj ikr fd;k

ml us $\frac{1}{2}$.kkRed fpE dks Nkmfsgq] muga fHkkukadu dh rjg foHkkftr fd;k vks ckn ea ikr
ifj.kke o] ikFk $\frac{1}{2}$.kkRed fpE yxk fn;k

nskaus, d gh eku $\frac{28}{45}$ ikr fd;k $\frac{2}{3}$ dks $\frac{5}{7}$ ls nskaofek;kjk Hkkx nadj nf[k,

fd D;k vki , d gh (Ieku) mukj ikr djrs g

nijks ls;g i{:k gksk gfd , d ifjes 1{:k dks fdlh vll; ifjes 1{:k ls
Hkkx nns o] fy,] ge ml ifjes 1{:k dks vll; ifjes 1{:k o 0; Øe ls xqkk dj
nss g

$$\text{bl idkj} \quad \frac{6}{5} \times \frac{2}{3} = \frac{6}{65} \times \frac{62}{3} dk 0; Øe \quad \frac{6}{5} \quad \frac{3}{2} \quad \frac{18}{10} g$$

iz kl dhft,

$$\frac{6}{11}, \frac{8}{5} o$$

0; Øe D;k gks



iz kl dhft,

$$\text{Kkr dhft, \% (i)} \quad \frac{2}{3} \quad \frac{7}{8} \quad \text{(ii)} \quad \frac{6}{7} \quad \frac{5}{7}$$



itukoyh 9.2

1. ;ks Kkr dñft, %



(i) $\frac{5}{4}$ $\frac{11}{4}$

(ii) $\frac{5}{3}$ $\frac{3}{5}$

(iii) $\frac{9}{10}$ $\frac{22}{15}$

(iv) $\frac{3}{11}$ $\frac{5}{9}$

(v) $\frac{8}{19}$ $\frac{2}{57}$

(vi) $\frac{2}{3}$ 0

(vii) $2\frac{1}{3}$ $4\frac{3}{5}$

2. Kkr dñft, %



(i) $\frac{7}{24}$ $\frac{17}{36}$

(ii) $\frac{5}{63}$ $\frac{6}{21}$

(iii) $\frac{6}{13}$ $\frac{7}{15}$

(iv) $\frac{3}{8}$ $\frac{7}{11}$

(v) $2\frac{1}{9}$ 6

3. xqkui ly Kkr dñft, %

(i) $\frac{9}{2}$ $\frac{7}{4}$

(ii) $\frac{3}{10}$ 9

(iii) $\frac{6}{5}$ $\frac{9}{11}$

(iv) $\frac{3}{7}$ $\frac{2}{5}$

(v) $\frac{3}{11}$ $\frac{2}{5}$

(vi) $\frac{3}{5}$ $\frac{5}{3}$

4. fuEufyf[kr oñ eku Kkr dñft, %

(i) (-4) $\frac{2}{3}$

(ii) $\frac{3}{5}$ 2

(iii) $\frac{-4}{5}$, (-3)

(iv) $\frac{1}{8}$ $\frac{3}{4}$

(v) $\frac{2}{13}$ $\frac{1}{7}$

(vi) $\frac{7}{12}$ $\frac{2}{13}$

(vii) $\frac{3}{13}$ $\frac{4}{65}$

geus D; k ppkz dh \

1. , d | ;k ft | s $\frac{p}{q}$ o : i e 0; Dr fd; k tk lo tgi p vlg q i wkkd gsrFkk q 0
g ifjes | ;k dgykrh g | ;k, i $\frac{2}{7}, \frac{3}{8}, 3$ bR; kfn ifjes | ;k, i g
2. | Hkh i wkkd vlg fHklu ifjes | ;k, i g
3. ;fn fd | h ifjes | ;k o vlg gj dks, d gh 'k; rj i wkkd | s xqkk fd; k
tk, ;k Hkkx fn; k tk,] rks ge, d ifjes | ;k i klr gkrh gS tks nh gB ifjes
| ;k o | er; ifjes | ;k dgh tkrh g mnkgj.kkFk] $\frac{3}{7} - \frac{3}{7} \frac{2}{2} - \frac{6}{14}$ g
vr% ge dgrs g fd $\frac{6}{14}$ | ;k $\frac{3}{7}$ dk, d | er; : i g | kfk gh] è;ku nhft,
fd $\frac{6}{14} - \frac{6}{14} \frac{2}{2} - \frac{3}{7}$ g
4. ifjes | ;kvka dks èkukRed vlg $\frac{1}{2}$.kkRed ifjes | ;kvka o : i eaoxhNr fd; k
tkrk g tc vlg vlg gj nksuka gh ;k rks èkukRed i wkkd gka; k $\frac{1}{2}$.kkRed i wkkd gk
rks og ifjes | ;k èkukRed ifjes | ;k dgykrh g tc vlg ;k gj e | s, d
 $\frac{1}{2}$.kkRed i wkkd gk rks og ifjes | ;k , d $\frac{1}{2}$.kkRed ifjes | ;k dgykrh g
mnkgj.kkFk] $\frac{3}{8}$, d èkukRed ifjes | ;k g srFkk $\frac{8}{9}$, d $\frac{1}{2}$.kkRed ifjes | ;k g
5. | ;k 0 u rks, d èkukRed ifjes | ;k gS vlg u gh $\frac{1}{2}$.kkRed ifjes | ;k g
6. , d ifjes | ;k dks vius ekud : i earc ekuk tkrk g tc ml dk gj èkukRed
i wkkd gksrFkk vlg vlg gj e 1 o vfrfjDr dkz lkoZxqku[kM u gka | ;k, i $\frac{1}{3}, \frac{2}{7}$,
bR; kfn ekud : i e g
7. nks ifjes | ;kvka o chp vI hfer ifjes | ;k, i gkrh g
8. Iku gj okyh nks ifjes | ;kvka dk ;k Kkr djus o fy,] muo vlg dks t kM
tk l drk gS rFkk gj ogh j[k dj ;k Kkr fd; k tk l drk g fHklu&fHklu gjka okyh
nks ifjes | ;kvka dks t kMuso fy,] i gysnksuka gjka dk y-l - Kkr fd; k tk rk gS vlg
fi 0j nksuka ifjes | ;kvka dks y-l - o cjkcj Iku gj okyh nks l er; ifjes
| ;kvka eacny dj t kMfy; k tk rk g mnkgj.kkFk] $\frac{2}{3} - \frac{3}{8} - \frac{16}{24} - \frac{9}{24} - \frac{16}{24} - \frac{9}{24} - \frac{7}{24}$
g ; gka 3 vlg 8 dk y- l - 24 g

9. nks ifjes $\frac{1}{4}$; kvk $\ddot{\text{a}}$ dk 0; odyu djus o $\ddot{\text{f}}$ fy, ge ?kvkbz tkus okyh ifjes $\frac{1}{4}$; k o $\ddot{\text{f}}$;k $\ddot{\text{t}}$; ifryke dks vU; ifjes $\frac{1}{4}$; k e $\ddot{\text{a}}$ tkMfs g $\ddot{\text{a}}$

$$\text{bl i $\ddot{\text{d}}$ kj] } \frac{7}{8} \frac{2}{3} \frac{7}{8} \frac{2}{3} \text{ dk ;k $\ddot{\text{t}}$; ifryke} = \frac{7}{8} \frac{(2)}{3} \frac{21}{24} \frac{(-16)}{24} \frac{5}{24} \text{ g $\ddot{\text{a}}$$$

10. nks ifjes $\frac{1}{4}$; kvk $\ddot{\text{a}}$ dk xqkk djus o $\ddot{\text{f}}$ fy,] ge bu $\frac{1}{4}$; kvk $\ddot{\text{a}}$ o $\ddot{\text{f}}$ v $\ddot{\text{a}}$ kkar Fkk gjk $\ddot{\text{a}}$ dk $\ddot{\text{a}}$
vyx&vyx xqkk djrs g $\ddot{\text{a}}$ v $\ddot{\text{a}}$ fi 0j xqkui ly dks $\frac{v\ddot{\text{a}}kka\text{ dk xqkui ly}}{gjk\text{ dk xqkui ly}}$ o $\ddot{\text{f}}$: i e $\ddot{\text{a}}$ fy [krs g $\ddot{\text{a}}$

11. ,d ifjes $\frac{1}{4}$; k dks, d vU; 'k $\ddot{\text{t}}$; s $\ddot{\text{r}}$ ifjes $\frac{1}{4}$; k l $\ddot{\text{s}}$ Hkkx nsis o $\ddot{\text{f}}$ fy,] ge i gyh ifjes $\frac{1}{4}$; k dks vU; ifjes $\frac{1}{4}$; k o $\ddot{\text{f}}$ 0; l $\ddot{\text{o}}$ e l $\ddot{\text{s}}$ xqkk djrs g $\ddot{\text{a}}$ bl i $\ddot{\text{d}}$ kj
- $$\frac{7}{2} \frac{4}{3} \frac{7}{2} \times \left(\frac{4}{3} \text{ dk } 0; l $\ddot{\text{o}}$ e \right) \frac{7}{2} \times \frac{3}{4} \frac{21}{8} \text{ g $\ddot{\text{a}}$$$

